Intraoperative mapping of the cortical areas involved in multiplication and subtraction: an electrostimulation study in a patient with a left parietal glioma

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Objectives: Advances in neuroimaging studies have recently improved the understanding of the functional anatomy of the calculation processes, having in particular underlined the central role of the angular gyrus (AG). In this study, the authors applied this knowledge to the surgical resection of a glioma invading the left AG, by localising and sparing the cortical areas involved in two different components of calculation (multiplication and subtraction), using direct electrical stimulations.

Methods: A calculation mapping was performed in a patient without deficit except a slightly impaired performance for serial arithmetic subtraction, during the resection under local anaesthesia of a left parieto-occipital glioma invading the dominant AG. After somatosensory and language mappings, cortical areas involved in single digit multiplications and subtractions of seven were mapped using the method of electrostimulation, before glioma removal.

Results: Distinct sites specifically involved in multiplication or subtraction were detected within the left AG, with a precise spatial distribution and overlapping. All the eloquent (somatosensory, language, and calculation) areas were surgically spared. Postoperatively, the patient had a transient complete deficit for arithmetic subtraction, without either multiplication or language disturbance. The tumour removal was complete.

Conclusions: These findings suggest: firstly, the usefulness of an intraoperative calculation mapping during the removal of a lesion involving the left dominant AG, to avoid permanent postoperative deficit of arithmetic processes while optimising the quality of tumour resection; secondly, the possible existence of a well ordered and dynamic anatomo-functional organisation for different components of calculation within the left AG.

Ever since Henschchen’s seminal study,1 evidence from neuropsychological reports in brain damaged patients2–8 and functional neuroimaging studies9–21 points toward a major involvement of inferior parietal regions in mental calculation. Moreover, there are indications that these areas include arithmetic components that may be selectively impaired or preserved following lesions.2, 3, 11–14, 17–21, 23, 26. Indeed, parietal damage can induce dissociated disorders of various types of calculation.2, 11–14 In the same way, acalculia may be isolated or associated with impairment of other cognitive functions,11 such as aphasia or Gerstmann’s syndrome.

Development of positron emission tomography and functional MRI, have recently improved the knowledge of the distributed networks that subserve calculation abilities, including prefrontal, premotor, and parietal cortices.7, 12, 15, 16, 17–20, 24, 25 In particular, a clear cut distinction is emerging between the left angular gyrus (AG) proper, showing more activation for language dependent calculation (multiplication and exact calculation), and a more anterior bilateral intraparietal site, showing greater activation during non-rote quantity manipulations (such as subtraction and approximate calculation).7, 11, 17, 20

In this report, we applied this knowledge to the surgical resection of a glioma invading the left AG, by performing under local anaesthesia an intraoperative electrostimulation mapping of the cortical areas involved in calculation processes. Our goals were first to avoid permanent postoperative calculation deficit, and to study the involvement of different left parietal regions in multiplication versus subtraction, two operations that can be doubly dissociated after parietal lesions. On the basis of these findings, the anatomo-functional organisation of the AG, its integration in calculation networks, and its interaction with language and working memory functions are discussed.

METHODS

Case presentation

Patient

The patient was a 44 year old right handed nurse. She was operated on in our institution for a left parieto-occipital low grade glioma that was causing partial seizures.

The preoperative clinical examination, performed by a neurologist, was normal. There was no visuospatial deficit. Language was unimpaired including spontaneous speech, word generation, repetition, picture naming, writing, and reading.

Assessment of calculating skills revealed that the patient was able to read Arabic numerals aloud, to write Arabic numerals to dictation, to compare pairs of single word and multi-words numerals, and to recite multiplication tables without any error. However, although written complex calculations (multi-digit addition, multiplication, subtraction, and division problems) were normal (100% of good answers), mental serial subtraction by seven was slightly impaired in comparison with the performance of the age matched controls (20% of errors on 10 items—that is, only 80% of good answers). Moreover, the number span was restricted to four items forward and two in the backward order.

Handedness was assessed using a standardised questionnaire.22 Hemispheric dominance for language was assessed with preoperative functional MRI using semantic fluency, covert sentence repetition, and story listening tasks.23

The preoperative anatomical MRI showed a left tumour located at the parieto-occipital junction, involving the superior
parietal lobe, and the postero-superior part of the angular gyrus (fig 1).

**Intraoperative electrostimulation technique**

Because of the location of the tumour in the dominant hemisphere, it was decided to perform awake, intraoperative functional mapping, before and during surgical resection, to minimize the risk of neurological sequelae. The patient gave her written informed consent.

The cortico-subcortical map was obtained using the method of electrostimulation previously described by the authors. Briefly, a 5 mm spaced tips bipolar probe delivering a biphasic current was applied during four seconds on the brain (pulse frequency of 60 Hz, single pulse phase duration of 1 ms, amplitude of 6 mA, Ojemann cortical stimulator, Radionics, Burlington, MA). Mapping under local anaesthesia was first performed in the central region, to identify the primary somatosensory areas (eliciting paraesthesias in the contralateral hemibody when stimulated). Then, we detected sites where stimulation induced speech arrest during self paced verbal counting (regularly in order from 1 to 10, and so on), or anomia or paraphasias during picture naming.

**Experimental calculation tasks**

Preoperative MRI and intraoperative ultrasonography showed that the tumour was located at the parieto-occipital junction with infiltration of the postero-superior part of the AG. Therefore, the areas involved in mental calculation were also mapped during surgery.

Because of time constraints during the awake surgical procedure, all the stimuli were only presented verbally and not also visually using Arabic digits. For the same reason, only multiplication and subtraction were studied, and not addition and division.

Thus, the patient was asked to perform two different calculation tasks:

1. Simple multiplication problems, for example, single digit multiplications systematically with one operand <6 (for instance 4×4; 3×7; 2×6; 5×8 ...). No complex multidigit multiplication was performed, essentially because of the fact that the electrical stimulation should not exceed four seconds to avoid intraoperative seizures—thus, necessitating that all the operations were presented and solved by the patient within this delay.

2. Subtraction of seven from one or two digit numbers (for example, 96−7, then 9−7 ...).

Multiplication and subtraction problems were alternated—three multiplications then three subtractions, and so on. During one “calculation block” (for instance three multiplications), one task was performed without stimulation, a second one performed during electrostimulation, and the third one again without any stimulation (to check if the patient was again able to solve the problem, especially when the previous stimulation had induced a disruption of calculation). The same problems were presented for both stimulated and non-stimulated trials, but never consecutively. For instance:

- then one “subtraction block”: 96−7 (without stimulation), then 9−7 (with stimulation), then 54−7 (without stimulation);
- again one “multiplication block”: 5×8 (without stimulation), then 4×4 (with stimulation), then 3×7 (without stimulation);
- again one “subtraction block”: 80−7 (without stimulation), then 96−7 (with stimulation), then 9−7 (without stimulation);
- and so on.

The patient was never informed when the brain was stimulated. The same cortical site was never stimulated successively twice, to avoid seizures. At each stimulation site, the patient performed three blocks of subtraction and three blocks of multiplication, for a total of three stimulated problems and six non-stimulated problems for each type of operation. The whole left parietal lobe exposed by the bone flap was mapped for calculation (supramarginalis gyrus, AG—both parts involved and non-involved by the glioma—, superior parietal lobule), except the areas previously demonstrated during the calculation task as inducing speech arrest when stimulated.

The tumour removal was conducted using these functional landmarks as boundaries of the resection, at the cortical as well as at the subcortical level, as stimulations were continuously performed all along the surgery to identify the eloquent pathways.

**Postoperative course**

At three days and seven days after the surgery, the patient underwent the same neurological examination as preoperatively.

In the numerical domain, she was asked:

- to read Arabic numerals aloud,
- to write Arabic numerals to dictation,
- to compare pairs of single word and multi-words numerals,
- to solve orally presented single digit multiplication problems mentally,
- to solve orally presented single digit and multi-digit subtraction problems mentally.

MRI was performed three hours after the surgical procedure to evaluate the quality of glioma resection.

**RESULTS**

**Intraoperative mapping**

The tumour was first delineated using ultrasonography, and boundaries marked by letter tags on the brain surface. The functional stimulation mapping then permitted identification of the following cortical sites (fig 2):

- primary somatosensory areas of the hand and fingers (tags 10, 11, 12), located within the retrocentral gyrus, in front of the intraparietal sulcus;
- a site located in the inferior part of the supramarginalis gyrus, where stimulations induced complete speech arrest (tag 20);
This report of an intraoperative calculation mapping during removal of the lesion, a subcortical pathway eliciting anomia when stimulated immediately before resection was identified all along the surgical procedure. Moreover, a subcortical pathway eliciting anomia when stimulated was identified deeply (40) at the level of the lateral wall of the ventricle (infero-anterior wall of the surgical cavity). An: anterior; P: posterior; M: midline; star: supramarginalis gyrus.

During removal of the lesion, a subcortical pathway eliciting anomia when stimulated was identified deeply (tag 40), at the level of the lateral wall of the ventricle (which was surgically opened). The resection was then stopped according to the functional cortico-subcortical boundaries provided by electrical stimulation, namely with removal of the entire superior parietal lobule, the posterior part of the inferior parietal lobule, and the anterior part of the occipital lobe that was invaded by the glioma (fig 3). White matter stimulation never induced any disruption of calculation.

**Postoperative course**

Three days after surgery, the patient had no motor or language disturbance (spontaneous speech, word generation, repetition, and naming were normal). The examination of sensory functions showed a slight impairment of proprioception in the right upper limb, and a right inferior quadrantanopia, hampering a precise visual guided reaching.

In the numerical domain, the patient was able to read and write Arabic numerals, and to compare pairs of single word and multi-words numerals without error. Single digit multiplication problems were solved without error but abnormally slowly (error rate, 0/10). Mental arithmetic subtraction was completely impossible, but in 50% of trials, the results were those of the corresponding addition (for example, 10 − 7 = 17 or even 4 − 2 = 6) (100% of error, 10 of 10), may be related to problems of attention.

Moreover, the numeral span was reduced to two items (impossible in the reversed order). At this time, the patient was too tired to undergo further testing.

Seven days after the surgical procedure, the somatic examination was normalised, except for the right inferior quadrantanopia. Before discharge, calculation tasks were performed. The patient was again able to read and write arabic numerals, and to compare pairs of single word and multi-words numerals without error. Single digit multiplication problems were solved more easily and faster than four days before, and without any error (error rate, 0 of 20). Subtraction problems were solved without any error (even serial subtractions like 100 − 7 = 17 . . .), except for the more complex multi-digit subtraction (for example, 47 − 13) with still an error rate of 40%.

Finally, the numeral span improved (four items forward and four in the reversed order, as preoperatively).

The immediate postoperative MRI showed a complete tumour removal, and confirmed the resection of the entire superior parietal lobule, the posterior part of the inferior parietal lobule, and the parieto-occipital junction (fig 4).

**DISCUSSION**

This report of an intraoperative calculation mapping during resection of a left parieto-occipital glioma underlines two points of interest: surgical and pathophysiological.
**Surgical interest**

Most recent series show that the regular use of the method of intraoperative brain electrostimulation during surgery in eloquent areas improved postoperative functional results.\(^{36–38}\) Currently, direct stimulations are a safe, precise, and reliable method to identify the cortical and subcortical eloquent areas indispensable for sensorimotor, and even cognitive functions in awake patients.\(^{15,20–22}\) Indeed, it was demonstrated for cognitive functions, particularly language, that stimulations induce a transient inhibition of the function when applied on the essential cerebral structures—both grey or white matter.\(^{23–25}\) However, very few attempts were made to map specifically calculation areas during surgery of lesion involving the left dominant parietal lobules, as only Whalen reported such an observation, testing only multiplication.\(^{26}\)

In this study, we showed that calculation processes involved in multiplication and subtraction could be transiently disrupted by direct cortical electrostimulation, permitting identification and sparing, during tumour removal, cortices essential for calculation. The results of intraoperative mapping were confirmed by the postoperative clinical course, as even though the patient had a transient deficit in subtraction (for which the cortical sites were the nearest to the surgical cavity), there was a recovery, proving that the all crucial calculation sites were preserved. Thus, the removal of an infiltrative glioma (to improve the quality of resection while minimising the risk of sequelae) can be considered using functional boundaries—represented not only by sensorimotor and language sites as previously described,\(^{31,32–34}\) but also by calculation areas.

Nevertheless, these preliminary findings need to be confirmed with larger number of patients, and extended by a more extensive intraoperative mapping of a wider variety of arithmetic tasks (that is, with incorporation of at least addition and division tasks)—with the aim to avoid any permanent postoperative calculation deficit after surgery of lesions involving the left parietal lobules (in particular the AG).

**Pathophysiological interest**

Calculation and the parietal lobe: the central role of the angular gyrus

Our intraoperative results clearly show that all the cortical sites whose stimulations elicited transient disruption of different forms of calculation were located exclusively within the AG. This finding supports the theory of Peritz and Henschen, who suggested that the left AG harboured a specific "calculation centre".\(^{1,44}\) Although this idea is not a new one, the use of electrostimulation has permitted confirmation of this hypothesis by a direct precise and reliable method. Indeed, deficits in calculation have been associated with a great variety of lesion locations in patients, and an overview of lesion studies led merely to the conclusions that left posterior cortical damage is more likely than anterior damage to affect mental calculation.\(^{10,26}\) The difficulty in demonstrating that the AG constitutes the functional (parietal) epicentre for number processing in brain damaged patient can be partly explained by the fact that many lesions involved several parietal structures (superior lobule, postcentral gyrus, supramarginalis gyrus, AG).\(^{27}\)

More recently, the development of functional neuroimaging methods improved the knowledge of distributed networks that subserve the performance of calculation tasks: activations during calculation tasks were tightly concentrated to the AG and the intraparietal sulcus.\(^{3,11–15,20}\) However, these non-invasive techniques do not permit clear differentiation of the cortical areas involved in calculation, from those really essential for this function. Consequently, electrostimulation data seem to represent a substantial complement to the knowledge of the organisation of arithmetical areas, as the method evaluates the effect of a transient, limited, "evolving" and not "fixed" lesion in the same patient performing alternately different types of calculation tasks. This permits identification of the eloquent sites indispensable for the function.

Therefore, even tendering into account the likely existence of an individual anatomofunctional variability,\(^{36,44–46}\) these results give further support in favour of a key role of the left AG in mental calculation. It is also noted that the intraoperative data have been supported by the postoperative course, namely the recovery of arithmetic processing despite a total resection of the superior parietal lobule.

Angular gyrus organisation: distribution of the distinct multiplication/subtraction areas

Our study also argues in favour of the existence of distinct calculation sites within the AG; a site specifically involved in rote multiplication, and a site specifically involved in subtraction—plus an intermediary area (overlapping of the two previous sites) involved in both processings.

Indeed, the use of intraoperative electrical stimulations permitted performance of an accurate mapping (5 mm of resolution) of the AG during two calculation tasks: multiplication and subtraction. Our results showed the existence of distinct anatomical sites specifically inhibited by stimulation during either multiplication or subtraction; a multiplication area in the inferior part of the AG, and subtraction area in the superior part immediately below the intraparietal sulcus and behind the supramarginalis gyrus. There was also an overlapping site for both functions (tag 31). Such an organisation was confirmed by the postoperative course, namely a transient but complete specific subtraction deficit (while the multiplication was slow but possible), after resection that came very close to the superior part of the angular gyrus. The patient also presented with 20% of errors during subtraction tasks, corresponding to a level of performance considered to be impaired compared with that of her age matched controls (probably because of the immediate vicinitiy of the corresponding cortical site with the tumour).

Interestingly, this distribution seems very similar to the somatotopy widely described within the primary motor area—that is, distinct representations for each movement\(^{47–49}\) but with overlapping permitting a dynamic organisation,\(^{50}\) corresponding to parallel networks that enable neuronal recruitment for complex motor sequences, new skill acquisitions,\(^{49}\) or functional recovery after damage.\(^{45}\)
Consequently, we hypothesise the existence within the angular gyrus of a possible dynamic “calculotopy”, based on a well-ordered distribution of specific calculation sites, nevertheless with overlapping.

Obviously, as a low grade glioma tends to be a slowly growing tumour, it cannot be certain that the functional re-organisation did not take place for calculation on this patient, as previously described for sensorimotor and language functions. However, our results seem in concordance with existing data from the literature: Cohen et al have described the case of a patient with multiplication problems despite subtraction preservation. The lesion affected the parietal perisylvian cortex, while a subset of the left inferior parietal lobule close to the intraparietal sulcus was spared; interestingly, this area could correspond to the superior part of the AG suggested to represent the “subtraction cortex” in our patient (tag 33).

Other authors also reported cases of patients who suffered from an intracranial haemorrhage at the left parieto-temporal junction, again with preservation of the superior part of the left inferior parietal cortex (near the intraparietal sulcus), with impairment in multiplication but not in subtraction.17 24

Secondly, a previous intraoperative calculation mapping study showed that electrostimulation of the left parietal lobe induced a transient deficit of the arithmetic processes.13 Although only multiplication was studied in this report, with no attempt made to dissociate the areas involved in the different components of mental calculation, it is interesting to note that the multiplication disturbances were induced during stimulation of the inferior parietal cortex located immediately above and behind the end of the Sylvian fissure,14 that is, very close to the “multiplication area” detected in our work (tag 30).

Thirdly, recent neuroimaging studies argued in favour of a dissociation between the left AG proper, activated in arithmetic fact (for example, in multiplication more than in subtraction15 16 and in exact more than in approximate calculation17 18), and a more anterior and intraparietal site activated more during actual calculation such as subtraction (potentially associated to a prefrontal and/or right parietal activation19 20 21 22 23). Our results fit very well with these data, as the “subtraction area” identified by stimulation in the present work is more anterior and superior (immediately below the intraparietal sulcus and at the junction with the supramarginal gyrus) than the “multiplication cortex” within the inferior part of the AG.

In conclusion, cortical areas involved in multiplication and subtraction seem to be distinct within the left AG, explaining that patients may be selectively impaired in one of these operations with preservation of the other one.1 3 5 17 22 24

CONCLUSIONS
These findings suggest:
- firstly, the usefulness of an intraoperative calculation mapping during the removal of lesion involving the left dominant AG, to avoid postoperative definitive deficit of arithmetic processing while optimising the quality of tumour resection;
- secondly, the possible existence of a well-ordered and dynamic anatomo-functional organisation for different components of calculation within the left AG.

However, we must underline the fact that the surgical and pathophysiological considerations reported in this work are based on a single patient. Consequently, further studies are mandatory to confirm these preliminary data, with:
- a larger number of patients;
- a greater number of intraoperative stimuli, testing more arithmetic processes such as addition and division;
- if possible, a correlation for each patient between the results of intraoperative electrical calculation mapping and those of preoperative and postoperative functional neuroimaging performed during the same tasks.

Moreover, transcranial magnetic stimulations could be used to simulate intraoperative electrical stimulation with normal control participants, to better understand the anatomo-functional organisation of calculation networks.

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Competing interests: none declared.

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